Measurement of the effective $B_s^0 \rightarrow K^+K^-$ lifetime

LHCb Collaboration

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A B S T R A C T

A measurement of the effective $B_s^0 \rightarrow K^+K^-$ lifetime is presented using approximately 37 pb$^{-1}$ of data collected by LHCb during 2010. This quantity can be used to put constraints on contributions from processes beyond the Standard Model in the $B_s^0$ meson system and is determined by two complementary approaches as

$$\tau_{KK} = 1.440 \pm 0.096 \text{ (stat)} \pm 0.008 \text{ (syst)} \pm 0.003 \text{ (model)} \text{ ps}. $$

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1. Introduction

The study of charmless $B$ meson decays of the form $B \rightarrow h^+h^-$, where $h^0$ is either a kaon, pion or proton, offers a rich opportunity to explore the phase structure of the CKM matrix and to search for manifestations of physics beyond the Standard Model. The effective lifetime, defined as the decay-time expectation value, of the $B_s^0$ meson measured in the decay channel $B_s^0 \rightarrow K^+K^-$ (charge conjugate modes are implied throughout the Letter) is of considerable interest as it can be used to put constraints on contributions from new physical phenomena to the $B_s^0$ meson system [1-4]. The $B_s^0 \rightarrow K^+K^-$ decay was first observed by CDF [5,6]. The decay has subsequently been confirmed by Belle [7].

The detailed formalism of the effective lifetime in $B_s^0 \rightarrow K^+K^-$ decay can be found in Refs. [3,4]. The untagged decay-time distribution can be written as

$$\Gamma(t) \propto (1 - A_{\Delta \Gamma}) e^{-\Gamma t} + (1 + A_{\Delta \Gamma}) e^{-\Gamma_L t}. $$

The parameter $A_{\Delta \Gamma}$ is defined as $A_{\Delta \Gamma} = -2 \text{Re}(\lambda)/(1 + |\lambda|^2)$ where $\lambda = (q/p)(\bar{A}/A)$ and the complex coefficients $p$ and $q$ define the mass eigenstates of the $B_s^0$-$\bar{B}_s^0$ system in terms of the flavour eigenstates (see, e.g., Ref. [8]), while $A$ ($A_{\bar{\Lambda}}$) gives the amplitude for $B_s^0$ ($\bar{B}_s^0$) decay to the CP even $K^+K^-$ final state. In the absence of CP violation, $\text{Re}(\lambda) = 1$ and $\text{Im}(\lambda) = 0$, so that the distribution involves only the term containing $\Gamma_L$. Any deviation from a pure single exponential with decay constant $\Gamma_L^{-1}$ is a measure of CP violation.

When modelling the decay-time distribution shown in Eq. (1) with a single exponential function in a maximum likelihood fit, it converges to the effective lifetime given in Eq. (2) [9]. For small values of the relative width difference $\Delta \Gamma/\Gamma = (\Gamma_L - \Gamma_L)/(\Gamma_L + \Gamma_L)/2$, the distribution can be approximated by Taylor expansion as shown in the second part of the equation [3]

$$\tau_{KK} = \tau_{B_s^0} \left( \frac{1}{1-y_s^2} \left[ 1 + 2A_{\Delta \Gamma} y_s + y_s^2 \right] \right)$$

$$= \tau_{B_s^0} \left( 1 + A_{\Delta \Gamma} y_s + O(y_s^2) \right),$$

where $\tau_{B_s^0} = 2/(\Gamma_H + \Gamma_L)$ and $y_s = \Delta \Gamma/2 \Gamma_s$. The Standard Model predictions for these parameters are $A_{\Delta \Gamma} = 0.97 \pm 0.004$ [3] and $y_s = 0.066 \pm 0.016$ [10].

The decay $B_s^0 \rightarrow K^+K^-$ is dominated by loop diagrams carrying, in the Standard Model, the same phase as the $B_s^0$-$\bar{B}_s^0$ mixing amplitude and hence the measured effective lifetime is expected to be close to $\Gamma_L^{-1}$. The tree contribution to the $B_s^0 \rightarrow K^+K^-$ decay amplitude, however, introduces CP violation effects. The Standard Model prediction is $\tau_{KK} = 1.390 \pm 0.032$ ps [3]. In the presence of physics beyond the Standard Model, deviations of the measured value from this prediction are possible.

The measurement has been performed using a data sample corresponding to an integrated luminosity of 37 pb$^{-1}$ collected by LHCb at an energy of $\sqrt{s} = 7$ TeV during 2010. A key aspect of the analysis is the correction of lifetime biasing effects, referred to as the acceptance, which are introduced by the selection criteria to enrich the $B$ meson sample. Two complementary data-driven approaches have been developed to compensate for this bias. One method relies on extracting the acceptance function from data, and then applies this acceptance correction to obtain a measurement of the $B_s^0 \rightarrow K^+K^-$ lifetime. The other approach cancels the acceptance bias by taking the ratio of the $B_s^0 \rightarrow K^+K^-$ lifetime distribution with that of $B^0 \rightarrow K^+\pi^-$. 

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2. Data sample

The LHCb detector [11] is a single arm spectrometer with a pseudorapidity acceptance of 2 < \eta < 5 for charged particles. The detector includes a high precision tracking system which consists of a silicon vertex detector and several dedicated tracking planes with silicon microstrip detectors (Inner Tracker) covering the region with high charged particle multiplicity and straw tube detectors (Outer Tracker) for the region with lower occupancy. The Inner and Outer trackers are placed after the dipole magnet to allow the measurement of the charged particles' momenta as they traverse the detector. Excellent particle identification capabilities are provided by two ring imaging Cherenkov detectors which allow charged pions, kaons and protons to be distinguished from each other in the momentum range 2–100 GeV/c. The experiment employs a multi-level trigger to reduce the readout rate and enhance signal purity: a hardware trigger based on the measurement of the energy deposited in the calorimeter cells and the momentum transverse to the beamline of muon candidates, as well as a software trigger which allows the reconstruction of the full event information.

B mesons are produced with an average momentum of around 100 GeV/c and have decay vertices displaced from the primary interaction vertex. Background particles tend to have low momentum and tend to originate from the primary pp collision. These features are exploited in the event selection. In the absolute lifetime measurement the final event selection is designed to be more stringent than the trigger requirements, as this simplifies the calculation of the candidate’s acceptance function. The tracks associated with the final state particles of the B meson decay are required to have a good track fit quality (\chi^2/n_{\text{dof}} < 3 for one of the two tracks and \chi^2/n_{\text{dof}} < 4 for the other), have high momentum (p > 13.5 GeV/c), and at least one particle must have a transverse momentum of more than 2.5 GeV/c. The primary proton–proton interaction vertex (or vertices in case of multiple interactions) of the event is fitted from the reconstructed charged particles. The reconstructed trajectory of at least one of the final state particles is required to have a distance of closest approach to all primary vertices of at least 0.25 mm.

The B meson candidate is obtained by reconstructing the vertex formed by the two-particle final state. The B meson transverse momentum is required to be greater than 0.9 GeV/c and the distance of the decay vertex to the closest primary pp interaction vertex has to be larger than 2.4 mm. In the final stage of the selection the modes B^0 \rightarrow K^+K^- and B^0 \rightarrow K^+\pi^- are separated by pion/kaon likelihood variables which use information obtained from the ring imaging Cherenkov detectors.

The event selection used in the relative lifetime analysis is very similar. However, some selection criteria can be slightly relaxed as the analysis does not depend on the exact trigger requirements.

3. Relative lifetime measurement

This analysis exploits the fact that the kinematic properties of the B^0 \rightarrow K^+K^- decay are very similar to those of B^0 \rightarrow K^+\pi^-.

The two different decay modes can be separated using information from the ring imaging Cherenkov detectors. The left part of Fig. 1 shows the invariant mass distribution of the B^0 \rightarrow K^+K^- candidates after the final event selection. In addition 1.424 B^0 \rightarrow K^+\pi^- candidates are selected. Using a data-driven particle identification calibration method described in the systematics section, the remaining contamination in the B^0 \rightarrow K^+K^- sample from other B \rightarrow h^+h^- final states in the analysed mass region is estimated to be 3.8%.

B mesons in either channel can be selected using identical kinematic constraints and hence their decay-time acceptance functions are almost identical. Therefore the effects of the decay-time acceptance cancel in the ratio and the effective B^0 \rightarrow K^+K^- lifetime can be extracted relative to the B^0 \rightarrow K^+\pi^- mode from the variation of the ratio R(t) of the yield of B meson candidates in both decay modes with decay time:

\[
R(t) = R(0)e^{-\left(t/t_{\text{eff}}\right)^2}. 
\]

The cancellation of acceptance effects has been verified using simulated events, including the full simulation of detector effects, trigger response and final event selection. Any non-cancelling acceptance bias on the measured lifetime is found to be smaller 1 fs.

In order to extract the effective B^0 \rightarrow K^+K^- lifetime, the yield of B meson candidates is determined in bins of decay time for both decay modes. Thirty bins between -1 ps and 35 ps are chosen such that each bin contains approximately the same number of B meson candidates. The ratio of the yields is then fitted as a function of decay time and the relative lifetime can be determined according to Eq. (3). With this approach it is not necessary to parametrise the decay-time distribution of the background. In order to maximise the statistical precision, both steps of the analysis are combined in a simultaneous fit to the K^+K^- and K^+\pi^- invariant mass spectra across all decay-time bins. The signal distributions are described by Gaussian functions and the combinatorial
background by first order polynomials. The parameters of the signal and background probability density functions (PDFs) are fixed to the results of time-integrated mass fits before the lifetime fit is performed. The $B^0 \to K^+\pi^-$ yield ($N_{B^0\to K^+\pi^-}$) is allowed to float freely in each bin but the $B^0 \to K^+K^-$ yield ($N_{B^0\to K^+K^-}$) is constrained to follow

$$N_{B^0\to K^+\pi^-}(\tau_i) = N_{B^0\to K^+\pi^-}(\bar{\tau}_i) e^{-\chi^2/2},$$

where $\tau_i$ is the mean decay time in the $i$th bin. In total the simultaneous fit has 94 free parameters and tests using Toy Monte Carlo simulated data have found the fit to be unbiased to below 1 fs on the measured $B^0 \to K^+K^-$ lifetime. Each mass fit used in the simultaneous fit is unbinned and must be split into mass bins in order to evaluate the fit $\chi^2$. Two mass bins are chosen, one signal dominated and one background dominated, in order to guarantee a minimum of 5–6 candidates in each bin. Using this approach the $\chi^2$ per degree of freedom of the simultaneous fit is found to be 0.82. The right part of Fig. 1 shows the decay-time distribution obtained from the fit and the fitted reciprocal lifetime difference is

$$\tau_{KK}^{-1} - \tau_{K\pi}^{-1} = 0.013 \pm 0.045 \text{ (stat) } \text{ps}^{-1}.$$

Taking the $B^0 \to K^+\pi^-$ lifetime as equal to the mean $B^0$ lifetime ($\tau_{B^0} = 1.519 \pm 0.007$ ps) [8], this measurement can be expressed as

$$\tau_{KK} = 1.490 \pm 0.100 \text{ (stat) } \pm 0.007 \text{ (input) } \text{ps},$$

where the second uncertainty originates from the uncertainty of the $B^0$ lifetime.

4. Absolute lifetime measurement

The absolute lifetime measurement method directly determines the effective $B^0 \to K^+K^-$ lifetime using an acceptance correction calculated from the data. This method was first used at the NA11 spectrometer at CERN SPS [12], further developed within CDF [13,14] and was subsequently studied and implemented in LHCb [15,16].

The per-event acceptance function is determined by evaluating whether the candidate would be selected for different values of the $B$ meson candidate decay time. For example, for a $B$ meson candidate, with given kinematic properties, the measured decay time of the $B$ meson candidate is directly related to the point of closest approach of the final state particles to the associated primary vertex. Thus a selection requirement on this quantity directly translates into a discrete decision about acceptance or rejection of a candidate as a function of its decay time.

This is illustrated in Fig. 2. In the presence of several reconstructed primary interaction vertices, the meson may enter a decay-time region where one of the final state particles no longer fulfills the selection criteria with respect to another primary vertex. Hence the acceptance function is determined as a series of step changes. These turning points at which the candidates enter or leave the acceptance of a given primary vertex form the basis of extracting the per-event acceptance function in the data. The turning points are determined by moving the reconstructed primary vertex position of the event along the $B$ meson momentum vector, and then reapplying the event selection criteria. The analysis presented in this letter only includes events with a single turning point. The drop of the acceptance to zero when the final state particles are so far downstream that one is outside the detector acceptance occurs only after many lifetimes and hence is safely neglected.

The distributions of the turning points, combined with the decay-time distributions, are converted into an average acceptance function (see Fig. 3). The average acceptance is not used in the lifetime fit, except in the determination of the background decay-time distribution.

The effective $B_s^0 \to K^+K^-$ lifetime is extracted by an unbinned maximum likelihood fit using an analytical probability density function (PDF) for the signal decay time and a non-parametric PDF for the combinatorial background, as described below. The measurement is factorised into two independent fits.

A first fit is performed to the observed mass spectrum and used to determine the signal and background probabilities of each event. Events with $B^0_s$ candidates in the mass range 5272–5800 MeV/c$^2$ were used, hence reducing the contribution of partially reconstructed background and contamination of $B^0$ decays below the $B^0_s$ mass peak. The signal distribution is modelled with a Gaussian, and the background with a linear distribution. The fitted mass value is compatible with the current world average [8].

The signal and background probabilities are used in the subsequent lifetime fit. The decay-time PDF of the signal is calculated analytically taking into account the per-event acceptance and the decay-time resolution. The decay-time PDF of the combinatorial background is estimated from data using a non-parametric method and is modelled by a sum of kernel functions which represent each candidate by a normalised Gaussian function centred at the measured decay time with a width proportional to an estimate of the density of candidates at this decay time [17]. The lifetime fit is performed in the decay-time range of 0.6–15 ps, hence only candidates within this range were accepted. The analysis was tested on the $B^0 \to K^+\pi^-$ channel, for which a lifetime compatible with the world average value was obtained, and applied to the $B_s^0 \to K^+K^-$ channel.
The analysis assumes that $B^0_s$ and $B^0$ mesons are produced in equal quantities. The influence of a production asymmetry for $B^0_s$ mesons on the measured lifetime is found to be small.

In the absolute lifetime method both a Gaussian and a Crystal Ball mass model [20] are implemented and the effect on fully simulated data is evaluated to estimate the systematic uncertainty due to the modelling of the signal PDF. In the relative lifetime method

$$
\tau_{KK} = 1.440 \pm 0.096 \text{ (stat) ps}
$$

and is illustrated in Fig. 3.

### 5. Systematic uncertainties

The systematic uncertainties are listed in Table 1 and discussed below. The dominant contributions to the systematic uncertainty for the absolute lifetime measurement come from the treatment of the acceptance correction (6.3 fs) and the fitting procedure (3.2 fs). The systematic uncertainty from the acceptance correction is determined by applying the same analysis technique to a kinematically similar high statistics decay in the charm sector ($D^0 \rightarrow K^+ \pi^-$ [18]). This analysis yields a lifetime value in good agreement with the current world average and of better statistical accuracy. The uncertainty on the comparison between the measured value and the world average is rescaled by the $B$ meson and charm meson lifetime ratio. The uncertainty due to the fitting procedure is evaluated using simplified simulations. A large number of pseudo-experiments are simulated and the pull of the fitted lifetimes compared to the input value to the fit is used to estimate the accuracy of the fit. These sources of uncertainty are not dominant in the relative method, and are estimated from simplified simulations which also include the systematic uncertainty of the mass model. Hence a common systematic uncertainty is assigned to these three sources.

The effect of the contamination of other $B \rightarrow h^+h^-$ modes to the signal modes is determined by a data-driven method. The misidentification probability of protons, pions and kaons is measured in data using the decays $K^0_s \rightarrow \pi^+\pi^-$, $D^0 \rightarrow K^+\pi^-$, $\phi \rightarrow K^+K^-$ and $A \rightarrow p\pi^-$, where the particle type is inferred from kinematic constraints alone [19]. As the particle identification likelihood separating protons, kaons and pions depends on kinematic properties such as momentum, transverse momentum, and number of reconstructed primary interaction vertices, the sample is reweighted to reflect the different kinematic range of the final state particles in $B \rightarrow h^+h^-$ decays. The effect on the measured lifetime is evaluated with simplified simulations.

Decays of $B^0_s$ and $B^0$ to three or more final state particles, which have been partially reconstructed, lie predominantly in the mass range below the $B^0_s$ mass peak outside the analysed region. Residual background from this source is estimated from data and evaluated with a sample of fully simulated partially reconstructed decays. The effect on the fitted lifetime is then evaluated.

In the absolute lifetime measurement, the combinatorial background of the decay-time distribution is described by a non-parametric function, based on the observed events with masses above the $B^0_s$ meson signal region. The systematic uncertainty is evaluated by varying the region used for evaluating the combinatorial background. In the relative lifetime measurement, the combinatorial background in the $hh'$ invariant mass spectrum is described by a first order polynomial. To estimate the systematic uncertainty, a sample of simulated events is obtained with a simplified simulation using an exponential function, and subsequently fitted with a first order polynomial.

Events may contain several primary interactions and a reconstructed $B$ meson candidate may be associated to the wrong primary vertex. This effect is studied using the more abundant charm meson decays where the lifetime is measured separately for events with only one or any number of primary vertices and the observed variation is scaled to the $B$ meson system.

Particle decay times are measured from the distance between the primary vertex and secondary decay vertex in the silicon vertex detector. The systematic uncertainty from this source is determined by considering the potential error on the length scale of the detector from the mechanical survey, thermal expansion and the current alignment precision.

The analysis assumes that $B^0_s$ and $B^0$ mesons are produced in equal quantities. The influence of a production asymmetry for $B^0_s$ mesons on the measured lifetime is found to be small.

In the absolute lifetime method both a Gaussian and a Crystal Ball mass model [20] are implemented and the effect on fully simulated data is evaluated to estimate the systematic uncertainty due to the modelling of the signal PDF. In the relative lifetime method

![Fig. 3. Left: Average decay-time acceptance function for signal events, where the error band is an estimate of the statistical uncertainty. The plot is scaled to 1 at large decay times, not taking into account the total signal efficiency. Right: Decay-time distribution of the $B^0_s \rightarrow K^+K^-$ candidates and the fitted functions. The estimation of the background distribution is sensitive to fluctuations due to the limited statistics. Both plots are for the absolute lifetime measurement. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this Letter.)](image-url)
this uncertainty is evaluated with simplified simulations and included in the fitting procedure uncertainty.

In the absolute $B^0 \rightarrow K^+ K^-$ lifetime measurement a cut is applied on the minimal reconstructed decay time. As the background decay-time estimation will smear this step in the distribution, a systematic uncertainty is quoted from varying this cut.

There is an additional uncertainty introduced if the result is interpreted using Eq. (2), as this expression does not take into account decay-time acceptance. This effect was studied using simplified simulations modelling the acceptance observed in the data and conservative values of $\Delta t = 0.1$ ps and $\Delta \Delta t = 0.6$. The observed bias with respect to the prediction of Eq. (2) is 3 fs. This effect is labelled “Effective lifetime interpretation” in Table 1 and is not a source of systematic uncertainty on the measurement but is relevant to the interpretation of the measured lifetime.

6. Results and conclusions

The effective $B^0 \rightarrow K^+ K^-$ lifetime has been measured in $pp$ interactions using a data sample corresponding to an integrated luminosity of 37 pb$^{-1}$ recorded by the LHCb experiment in 2010. Two complementary approaches have been followed to compensate for acceptance effects introduced by the trigger and final event selection used to enrich the sample of $B^0$ mesons. The absolute measurement extracts the per-event acceptance function directly from the data and finds:

$$\tau_{KK} = 1.440 \pm 0.096 \text{ (stat)} \pm 0.008 \text{ (syst)} \pm 0.003 \text{ (model) ps}$$

where the third source of uncertainty labelled “model” is related to the interpretation of the effective lifetime.

The relative method exploits the fact that the kinematic properties of the various $B \rightarrow h^+ h^-$ modes are almost identical and extracts the $B^0 \rightarrow K^+ K^-$ lifetime relative to the $B^0 \rightarrow K^+ \pi^-$ lifetime as:

$$\tau_{KK}^{-1} - \tau_{K\pi}^{-1} = 0.013 \pm 0.045 \text{ (stat)} \pm 0.003 \text{ (syst)} \pm 0.001 \text{ (model) ps}^{-1}.$$ 

Taking the $B^0 \rightarrow K^+ \pi^-$ lifetime as equal to the mean $B^0$ lifetime ($\tau_B = 1.519 \pm 0.007$ ps) [8], this measurement can be expressed as:

$$\tau_{KK} = 1.490 \pm 0.100 \text{ (stat)} \pm 0.006 \text{ (syst)} \pm 0.002 \text{ (model)} \pm 0.007 \text{ (input) ps},$$

where the last uncertainty originates from the uncertainty of the $B^0$ lifetime. Both measurements are found to be compatible with each other, taking the overlap in the data analysed into account.

Due to the large overlap of the data analysed by the two methods and the high correlation of the systematic uncertainties, there is no significant gain from a combination of the two numbers. Instead, the result obtained using the absolute lifetime method is taken as the final result. The measured effective $B^0 \rightarrow K^+ K^-$ lifetime is in agreement with the Standard Model prediction of $\tau_{KK} = 1.390 \pm 0.032$ ps [3].

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